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## A numerical study of enhanced lithium-ion battery cooling using a module insert

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### ABSTRACT

Thermal performance of an electric vehicle (EV) battery module with an integrated cooling insert was numerically analyzed using computational fluid dynamics (CFD). Twelve NCM prismatic cells were packaged into a module where each cell was physically isolated from its neighboring cells by the cooling insert, designed to enhance the module's thermal performance. The battery cells and the cooling insert were attached to a thermal interface material (TIM) and a cooling plate with integrated liquid cooling where the coolant was a 50/50 ethylene glycol water (EGW) mixture. A heat generation model based on the discharge rate was used to assess the thermal responses of the module such as heat flux and temperature distribution. Thermal characteristics were studied under various discharge rates, coolant flow rates, insert thicknesses and material conditions. Results showed that the cooling insert reduced the cell temperature by 1.4 °C and increase the heat flux by 15.6% at 3 mm thickness with a coolant flow rate of 4 L/min. Cooling plates with plastic and metallic material properties were also studied and temperatures reductions up to 0.7 and 1.0 °C were observed, respectively. Furthermore, temperature uniformity was maintained to within 0.3 °C across all twelve cells at a coolant flow rate of 9 L/min. The results of this study could potentially lead to the development of a compact and low-cost intra-cell heat spreader in a battery module that can be readily implemented in production EVs.

### 1. Introduction

The automotive industry is undergoing a once in a century paradigm shift as increasing environmental regulations and public interest push many manufacturers from internal combustion engines and fossil fuels to electric motors and batteries [1,2]. As such, research into improving the performance and efficiency of electric powertrain and energy storage for automotive applications have significantly increased [3]. In particular, advanced battery technologies such as LiFePO<sub>4</sub> (LFP) and cobalt-based Li-ion batteries have significantly increased the energy storage capacities of battery electric vehicles (BEVs) [4]. LFP batteries have lower energy densities but have higher thermal tolerance compared to other Li-ion batteries, the latter of which is one of the reasons why they are widely used in Chinese BEVs. NMC Li-ion batteries, on the other hand, have higher energy densities [5] thereby enabling more efficient and longer range vehicles, but are more susceptible to heat compared to LFP batteries [6].

Despite many benefits, improved performance of any Li-ion batteries may be undermined if they are subject to less-than ideal operating conditions [7]. For example, battery chemistry can be very sensitive to temperature [8,9]. Lower than optimal temperatures reduce electrochemical reaction rates thereby decreasing battery capacity [10], whereas higher than optimal temperatures

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**Nomenclature**

$V$	voltage [V]
$V_o$	open circuit voltage [V]
$R$	internal resistance [ $\Omega$ ]
$\Delta S$	entropy change [ $\text{J K}^{-1} \text{mol}^{-1}$ ]
$F$	Faraday constant [ $\text{s A mol}^{-1}$ ]
$I$	current [A]
$T$	temperature [K]
$n$	number of transferred electron
$p$	pressure [Pa]
$\dot{Q}$	heat generation [W]
$t$	time [s]
$c_p$	specific heat [ $\text{J kg}^{-1} \text{K}^{-1}$ ]
$Re$	Reynolds number ( $Re = \rho \cdot v \cdot D_h \cdot \mu^{-1}$ )
$D_h$	hydraulic diameter [m]
$h$	convective heat transfer coefficient [ $\text{W m}^{-2} \text{K}^{-1}$ ]
$\rho$	density [ $\text{kg m}^{-3}$ ]
$\nu$	kinematic viscosity [ $\text{m}^2 \text{s}^{-1}$ ]
$\lambda$	heat transfer coefficient [ $\text{W m}^{-1} \text{K}^{-1}$ ]
$\mu$	viscosity [ $\text{kg m}^{-1} \text{s}^{-1}$ ]
$gen$	heat generation
$irr$	irreversible heat generation
$rev$	reversible heat generation
$EGW$	ethylene glycol Water
$TIM$	thermal interface material
$LIB$	lithium-ion battery
$BEV$	battery electric vehicle
$BTMS$	battery thermal management system
$CFD$	computational fluid dynamics
$EV$	electric vehicle
$LFP$	Lithium Iron Phosphate
$NMC$	Nickel Manganese Cobalt
$OCV$	open-circuit voltage
$PCM$	phase change material
$PHEV$	plug-in hybrid electric vehicle
$SOC$	state of charge
$SOH$	state of health

may increase unwanted reaction rates which ultimately reduce battery life and may even induce thermal runaway [11]. Internal defects and high charge/discharge rates can further induce higher internal heat generation thereby exacerbating thermal runaway. Furthermore, temperature variations across multiple battery cells within a module or a pack can induce internal resistance and capacity variations, ultimately resulting in reduced performance and inaccurate assessment of state of charge (SOC) and state of health (SOH) [12,13]. As such, a proper control of cell temperature and heat dissipation through a battery thermal management system (BTMS) is critical to battery lifespan, performance, and efficiency optimization [14–18]. A BTMS is designed to regulate a safe and optimal operating temperature, between 25 and 40 °C, and minimize temperature variation, to within several °C, across all cells in the module or pack.

Various techniques for regulating automotive battery temperatures based on air cooling [19–21], liquid cooling [22–24] and phase change material (PCM) [25,26] are being actively studied. Most air cooling techniques use fans to induce air flow over the battery and remove excess thermal energy. The heat transfer coefficient of the induced forced convection will depend on various factors such as air flow rate and surface area. Wang et al. [27] studied the effect of 18,650 Li-ion battery cell arrangement structures and fan placements on air cooling performance. The aforementioned studies compared various cell arrangement and found that an axisymmetric module provided the best air cooling performance, a rectangular module was the most cost-effective, and a hexagonal module was the most space-efficient. Also, fans mounted above the battery module produced the most effective air cooling regardless of the battery module design. Mahamud et al. [28] studied a reciprocating air flow duct to reduce temperature variations of an air-cooled battery system. A 120 s periodic air flow reciprocation reduced the temperature variation by 4 °C (72%), and reduced the

maximum cell temperature by 1.5 °C. Saw et al. [29] improved the cooling of circular 38,120 LFP cells by developing a duct that wraps around the battery cells and taking advantage of the compression and expansion of the air flow in the duct. Also, steady state 3D temperature distribution of the battery cells under various air flow rates were calculated using conjugate heat transfer (CHT) [30]. Numerical results identified a correlation between the Nusselt and the Reynolds number. However, cell temperatures exceeded the safe operating limit at high discharge rates and the authors suggested the use of higher air flow rates or liquid cooling.

In general, liquid cooling is preferred at higher battery capacities or charge/discharge rates. Huo et al. [31] suggested that a battery module be sandwiched between two liquid-cooled plates. Various factors including the number of cooling channels embedded into each cooling plate, flow rate, flow direction, external temperature were analyzed to determine the optimal cooling configuration. Results showed that liquid cooling was effective only when the external temperature did not exceed 35 °C. Liquid cooling channel configuration and coolant developments are also being actively researched, both experimentally and numerically. Pandchal et al. [32] and Jin et al. [33] studied liquid cooling using mini-channels and ultra-thin minichannels, respectively. Jarrett et al. [34] optimized a serpentine-channel cooling plate in which 18 design parameters were analyzed to optimize for coolant pressure drop, average temperature and temperature uniformity. Yang et al. [35] determined that liquid metal cooling produced a lower cell temperature and improved thermal uniformity compared to water cooling given the same flow rate condition. This is due to the much higher thermal conductivity of the liquid metal compared to water. Sefidan et al. [36] submerged a cylindrical Li-ion cell in coolant imbued with aluminium oxide nanoparticles and determined the cooling performance. Other researchers [37–43] compared the thermal transport phenomena of various nanofluids with water

Lastly, phase change material (PCM) is another promising thermal management technique that is being actively researched. Thermal equilibrium analyses have shown that PCM is more effective compared to air and liquid cooling [44–46]. Among various PCMs that are being considered for automotive battery thermal management, paraffin is the most suitable. However, as with most PCMs it has a relatively low thermal conductivity [47] and PCMs are usually applied in conjunction with air or water cooling. Ling et al. [48] compared the PCM cooling performance with and without forced air cooling and determined the hybrid cooling system (PCM with air cooling) to be more effective and maintained the temperature to within safe operating limits. Sabbah et al. [49] studied a PCM and air cooling system for small Li-ion batteries in PHEVs under various conditions such as discharge rate, cell temperature, and external temperature. The cell temperature did not exceed 55 °C even at an external temperature and discharge rate of 45 °C and 6.67C, respectively, without additional power draw for the cooling system.

The aforementioned studies represent only a fraction of the overall automotive battery thermal management strategy research. In many cases, however, the focus is to maximize temperature reduction using advanced cooling methods which may not be feasible in production vehicle environment where spaces are very limited and cost is prohibitive. It is therefore critical that a compact and inexpensive battery module technique is developed that can be integrated into existing design with minimal modifications. However, such studies are difficult to find in literature and so this study proposes a module-level battery cooling system that has a very small footprint and can be readily integrated into a high energy density battery packs in production EVs. In this study, a battery module containing 12 prismatic  $\text{Li}[\text{Ni}_{1/3}\text{Co}_{1/3}\text{Mn}_{1/3}]\text{O}_2$  Li-ion cells were analyzed under various flow rates, discharge rates, cooling insert dimensions and materials using CFD. The thermal responses of the module such as temperature and heat flux distribution across the module were used to evaluate the effectiveness of the integrated cooling insert.

## 2. Methods

### 2.1. Battery module model

Li-ion battery packs used in BEVs are mostly cell-module-pack structures where a group of battery cells are made into modules and a group of modules are made into battery packs. Most studies treat a battery module in a pack as an integral unit [50] and as such all thermal analyses in this study was performed at the module level. The module is made up of 12 cells, a cooling insert, a thin thermal interface material (TIM), and a cooling plate with integrated cooling jacket. The cooling insert is a guide structure with 12 slots, one for each cell, that is designed to enhance the thermal performance of the module. It is open at the top and the bottom so that cells can be easily removed and be in direct contact with the TIM. Once a cell has been placed in a slot it is physically isolated from its neighboring cells. Heat generated by the cell's side and bottom surfaces are conducted to the cooling plate through the cooling insert and the TIM, respectively. Convection through the U-shaped cooling jacket ultimately removed the heat from the module into its surroundings. The coolant is a 50/50 Ethylene Glycol Water (EGW) mixture, a common coolant in automotive applications. A 3D model of the module and the dimensions for the cooling plate are provided in Fig. 1.

### 2.2. Li-ion cell heat generation model

Twelve 37Ah prismatic lithium-ion battery cell were individually modeled for this study. The anode and cathode were graphite and NCM, respectively. The electrolyte was made up of lithium hexafluorophosphate. Detailed battery specifications [51] and thermodynamic properties [52] of the module components are provided in Table 1 and 2, respectively. Battery discharge rates are usually given by the C-rate and is based on  $I_t = C/1\text{h}$  as defined in the IEC61434 standard [29].  $I_t$  represents the discharge current during one hour discharge and  $C$  is the nominal capacity of a battery cell. C-rate is a multiple of  $I_t$ , such that higher C-rate corresponds to higher discharge rate, and shorter operating time. Conversely, lower C-rates (1/5–1/10 is typical in highway driving) corresponds to lower discharge rate, and longer operating time.

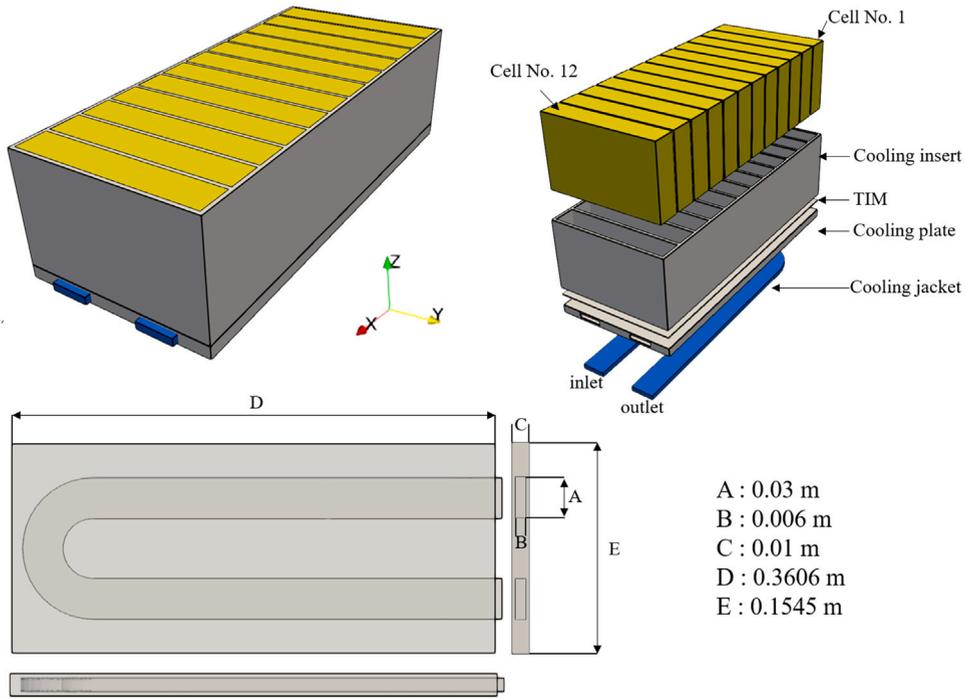


Fig. 1. Schematic and dimensions of the battery module and its components.

Table 1

Battery cell specifications.

Properties	Specification
Nominal capacity [Ah]	37
Nominal voltage [V]	3.7
Operating voltage [V]	2.8–4.2
Specific heat [J kg <sup>-1</sup> K <sup>-1</sup> ]	1100
Thermal conductivity [W m <sup>-1</sup> K <sup>-1</sup> ]	1.96:22.4:22.4
Size [mm]	91.6×148.5×26.8
Density [kg m <sup>-3</sup> ]	2630
Mass [kg]	0.82

Table 2

Thermodynamic properties of the battery module components and the coolant.

Property	Cooling insert & plate	TIM	Coolant
Thermal conductivity [W m <sup>-1</sup> K <sup>-1</sup> ]	237	3	0.4108
Density [kg m <sup>-3</sup> ]	2702	2700	1050.44
Specific heat [J kg <sup>-1</sup> K <sup>-1</sup> ]	903	1000	3499
Viscosity [kg m <sup>-1</sup> s <sup>-1</sup> ]			1.538 × 10 <sup>-3</sup>

The two major sources of internal heat generation in a Li-ion battery cell are irreversible heat generation due to internal battery resistance and reversible heat generation due to entropy change [9]. Therefore, the total heat generated by each cell for a given C-rate can be calculated using models of internal resistance and entropy variations as a function of SOC as shown in Eq. (1),

$$\dot{Q}_{gen} = \dot{Q}_{irr} + \dot{Q}_{rev} = I(V_o - V) - IT \frac{dV_o}{dT} = I^2R - T \Delta S \frac{I}{nF}. \quad (1)$$

where  $V_o$  is the open circuit voltage (OCV),  $V$  is the cell voltage,  $R$  is the internal resistance of battery,  $\Delta S$  is the changes of entropy,  $F$  is the Faraday constant (96485.4 C/mol). The model for internal resistance as a function of SOC can be found in Yang et al. [51]. The model for entropy change in an NCM-graphite lithium-ion battery can be found in Viswanathan et al. [53]. Overall, Eq. (1) can be represented as a function of SOC, wherein the SOC is expected to decrease linearly as a function of time at a given C-rate. Furthermore, since the current and voltage is a function of the SOC under constant C-rate, the above equation can be treated as a battery cell heat generation model as a function of time during discharge.

These models were used to perform transient analyses of 1C through 3C discharge cycles. The average heat generations at C-rates from 1C through 3C are provided in Table 3. These values were used to calculate the steady state temperature distribution and heat

**Table 3**  
Average cell heat generation under various C-rates.

1C	2C	3C	4C	5C
1.95 W	7.06 W	15.33 W	26.76 W	41.35 W

flux under various C-rates, coolant flow rates, cooling insert materials and thicknesses. Transient analyses result under 1C and 2C discharge rates agreed very well with their respective steady-state results due to relatively mild heat generation. Transient results under 3C discharge rate showed slightly higher temperature discrepancy (up to 1°C in cell 8) compared to its steady-state solution. Due to minimal difference between the transient and steady-state results, all subsequent results have been calculated using the steady-state assumption.

### 2.3. Governing equations

Heat conduction in each battery cell, the cooling insert, the TIM, and the cooling plate as well as conduction and convection in the coolant were calculated using the following continuity, momentum, and energy equations [54]

$$\text{Continuity equation: } \frac{\partial \rho}{\partial t} + \frac{\partial u_i}{\partial x_i} = 0, \quad (2)$$

$$\text{Momentum equation: } \frac{\partial(\rho u)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} (2\mu S_{ij} - \overline{\rho u_i' u_j'}), \quad (3)$$

$$\text{Energy equation: } \frac{\partial(\rho c_p T)}{\partial t} + \frac{\partial(\rho c_p u_j T)}{\partial x_j} = \frac{\partial}{\partial x_j} (\lambda \frac{\partial T}{\partial x_j} - \overline{\rho u_i' T'}) + Q_{gen}. \quad (4)$$

where  $u$  is velocity,  $\rho$  is density,  $p$  is pressure,  $Q_{gen}$  is heat generation,  $S_{ij} = \frac{1}{2}(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i})$ ,  $\nu$  is kinematic viscosity,  $\lambda$  is heat transfer coefficient,  $c_p$  is specific heat,  $\overline{u_i' u_j'}$  is Reynolds stress, and  $\overline{u_i' T'}$  is turbulent heat flux. The range of the Reynolds number in this study was between 630 and 7560. For turbulent flows, an improved two-equation eddy-viscosity turbulence model [55] and the hybrid wall model was used to calculate all layers near and far away from the wall for all flow conditions. Coefficients for the turbulence model can be found in [56].

$$\frac{\partial(\rho k)}{\partial t} + \frac{\partial(\rho u_j k)}{\partial x_j} = \tilde{P}_k - \beta^* \rho k \omega + \frac{\partial}{\partial x_j} \left[ (\mu + \sigma_k \mu_t) \frac{\partial k}{\partial x_j} \right], \quad (5)$$

$$\frac{\partial(\rho \omega)}{\partial t} + \frac{\partial(\rho u_j \omega)}{\partial x_j} = \alpha \rho S^2 - \beta \rho \omega^2 + \frac{\partial}{\partial x_j} \left[ (\mu + \sigma_\omega \mu_t) \frac{\partial \omega}{\partial x_j} \right] + 2(1 - F_1) \frac{\rho \sigma_\omega 2}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j}. \quad (6)$$

### 2.4. Numerical model: 3D model

Hexahedron mesh for each 3D models were created using the snappyhexmesh utility included in OpenFOAM. Finer mesh was applied near areas with high temperature gradients such as near boundaries and interfaces. Mesh independence was confirmed by comparing the maximum and minimum battery module temperatures using the same model under various mesh configuration from 3.1 to 26 million cells. Generally, numerical simulation is performed using an optimal number of mesh that provides a good balance of computational accuracy and cost. To that end, around 12 million meshes were used to model the temperature response of all 12 cells, cooling insert, TIM, cooling plate, and coolant in this study. The  $y+$  value was kept under 1 and 10 for transition and turbulent flows at higher flow rates, respectively.

### 2.5. Numerical solver: OpenFOAM

Thermofluidic analyses of the battery module and its cooling system were conducted using OpenFOAM [57], a popular opensource CFD package with a worldwide user base. CFD is used to model a wide range of fluid flows and heat transfer applications [58,59]. A conjugate heat transfer solver (chtMultiRegionSimpleFoam in OpenFOAM 8) was used to calculate the 3D heat conduction in solids as well as conduction and convection in the coolant. The coolant inlet pressure gradient was set to a fixed value determined by the flow rate. The coolant outlet pressure was fixed at atmospheric pressure. The initial battery module and coolant temperatures were set to 25 °C. Exterior side walls of the cooling insert and the top of the module were cooled via natural convection ( $h = 5 \text{ W m}^{-2} \text{ K}^{-1}$ ). The averaged heat generation values (Table 3) were used for steady state analyze.

## 3. Results and discussions

Temperature distributions within the module were calculated under various cooling insert thicknesses and materials, C-rates, and coolant flow rate conditions to gauge the maximum and minimum cell temperatures as well as the module temperature uniformity. Furthermore, heat flux were also calculated to compare the thermal performance of various cooling insert properties.

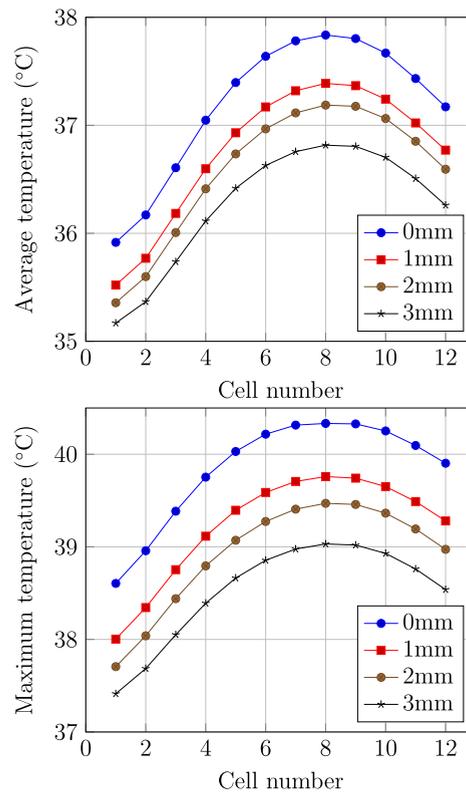


Fig. 2. (TOP) Average and (BOTTOM) maximum cell temperatures during 3C discharge rate and 4 L/min coolant flow rate.

Table 4  
Average temperature data from Fig. 2.

	0 mm [°C]	1 mm [°C]	2 mm [°C]	3 mm [°C]
Cell 1	35.9	35.5	35.3	35.2
Cell 2	36.2	35.8	35.6	35.4
Cell 3	36.6	36.2	36.0	35.7
Cell 4	37.0	36.6	36.4	36.1
Cell 5	37.4	36.9	36.7	36.4
Cell 6	37.6	37.2	37.0	36.6
Cell 7	37.8	37.3	37.1	36.7
Cell 8	37.8	37.4	37.2	36.8
Cell 9	37.8	37.4	37.2	36.8
Cell 10	37.7	37.2	37.1	36.7
Cell 11	37.4	37.0	36.8	36.5
Cell 12	37.2	36.8	36.6	36.3

### 3.1. Effect of cooling insert thickness on module temperatures

The thermal performance of the battery module was analyzed for various cooling insert thicknesses from 0 to 3 mm. 0 mm thickness refers to a condition in which no cooling insert was used in the module. Material properties of aluminium were used to model the cooling insert in this analysis. Average and maximum temperatures of all 12 cell are presented for 4 cooling insert thicknesses in Fig. 2 and Tables 4 and 5.

Steady state calculations were performed under 3C discharge rate and 4 L/min coolant flow rate. In all tested cases, the averaged and maximum temperatures were observed at cell 8 and decreased monotonically outwards towards cells 1 and 12. Recall that cell 1 was near the U-shaped bend in the cooling jacket and cell 12 was near the inlet and outlet of the cooling jacket. The slight skew in the averaged and maximum temperature distribution is driven by the cooling jacket geometry. Cells 1 and 12 also benefits from additional natural convection, but cell 1 temperatures are significant lower since it makes more contact with the U-shaped cooling jacket. Even cells 2 and 3 temperatures are lower than that of cell 12 for the same reason.

Cooling insert thickness also had significant impact on module temperatures. Results presented in Fig. 2 show decreasing averaged and maximum temperatures with thicker cooling inserts likely due to increased heat capacity of the added material.

**Table 5**  
Maximum temperature data from Fig. 2.

	0 mm [°C]	1 mm [°C]	2 mm [°C]	3 mm [°C]
Cell 1	38.6	38.0	37.7	37.4
Cell 2	39.0	38.3	38.0	37.7
Cell 3	39.4	38.8	38.4	38.0
Cell 4	39.8	39.1	38.8	38.4
Cell 5	40.0	39.4	39.1	38.7
Cell 6	40.2	39.6	39.3	38.9
Cell 7	40.2	39.7	39.4	39.0
Cell 8	40.3	39.8	39.5	39.0
Cell 9	40.3	39.7	39.5	39.0
Cell 10	40.2	39.7	39.4	38.9
Cell 11	40.0	39.5	39.2	38.8
Cell 12	39.9	39.3	39.0	38.6

**Table 6**  
Heat flux from the cooling insert to the TIM.

Cooling insert thickness	0 mm	1 mm	2 mm	3 mm
Heat flux from cooling insert [W m <sup>-2</sup> ]		29.47	61.03	93.17
Total heat flux into TIM [W m <sup>-2</sup> ]	444.3	465.8	489.3	514.0

**Table 7**  
Thermal properties of cooling insert materials.

Materials	Plastic	Copper	Aluminium
Thermal conductivity [W m <sup>-1</sup> K <sup>-1</sup> ]	0.163	398	237
Density [kg m <sup>-3</sup> ]	1070	8930	2700
Specific heat [J kg <sup>-1</sup> K <sup>-1</sup> ]	1990	385	903

A 3 mm cooling insert reduced the average and maximum temperatures by more than 2 °C across all cells compared to a module without an insert. Maximum temperatures remained below 40 °C for all cells even with a 1 mm cooling insert at a discharge rate of 3C. However, 7 out of 12 cells reported maximum temperatures in excess of 40 °C if no cooling insert was implemented (0 mm). This is due to the cooling insert heat capacity increasing with thickness thereby improving the cooling performance of the module. Furthermore, the cooling insert had a much higher thermal conductivity compared to a battery cell enabling a more efficient cooling.

The cooling insert also prevents direct heat conduction between neighboring battery cells and increases the heat transfer area from the cells to the TIM. Steady state heat flux from a 3 mm cooling insert to the TIM at a discharge rate of 3C ranged from 6 to 10 kW/m<sup>2</sup>, where sections that overlap the cooling jacket registered the highest heat flux. Direct heat flux from a battery cell to the TIM range from 4 to 8 kW/m<sup>2</sup>, lower than those of the cooling insert.

Heat flux can quickly scale up at higher discharge rates which further increase the need for a cooling insert. Positive heat flux from the cell to the insert can be observed in the upper sections of the insert away from the TIM. Heat transfer from the insert to the TIM in the lower one-fifth of the insert, closer to the TIM but at a much higher rate. Results show that heat generated in most areas of a cell is conducted into the cooling insert. Only a small portion of the battery (near the TIM) conducts heat directly into the TIM. Intense heat conduction between the cooling insert and the TIM was also observed near their intersections. The total heat flux from the cooling insert to the TIM at thicknesses from 1 to 3 mm are listed in Table 6. Results show a linear increase in heat flux as the cooling insert thickness increases indicating improved cooling performance. A 3 mm cooling insert increased the total heat flux by 70 W/m<sup>2</sup> or 15.6% compared to a module without a cooling insert.

### 3.2. Effect of cooling insert material on module temperatures

The thermal performance of a battery module was analyzed for various cooling insert materials such as aluminium, copper, and plastic. Material properties of the aforementioned materials are listed in Table 7. Steady state calculations are performed using a 3 mm thick cooling insert, 3C discharge rate and 4 L/min coolant flow rate (see Table 8). Average temperatures of all 12 cell are presented for plastic, aluminium, and copper in Fig. 3.

Overall, the use of any cooling insert produced lower cell temperatures by a minimum of 0.7 °C compared to a module without a cooling insert. Even the plastic cooling insert, despite having a lower thermal conductivity than the battery cell, resulted in lower cell temperatures. Among the three tested material, copper achieved the lowest average cell temperatures across all 12 cells. The aluminium cooling insert performance was very similar to that of copper, with an average cell temperature difference of about 0.15 °C. The plastic cooling insert produced the hottest cell temperatures by up to 0.56 °C compared to copper. Despite significant differences in thermal conductivity between metallic and plastic cooling inserts, temperature differences between the copper and plastic cooling insert was relatively small. This is likely due to plastic having much higher specific heat than aluminium or copper.

Temperature uniformity is also impacted by the cooling insert material. Cells in metallic cooling inserts had a temperature variation of 1.64 °C between the hottest and coldest cells. The variation increased to 1.9 °C for the plastic cooling insert.

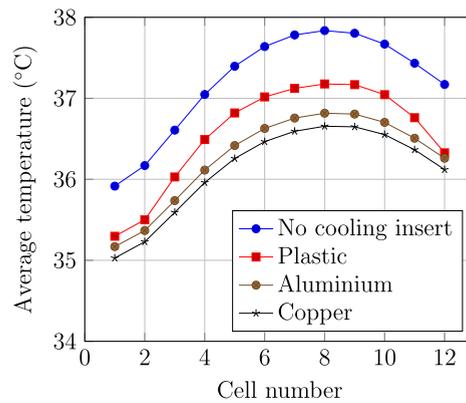


Fig. 3. Average cell temperatures for various cooling insert material.

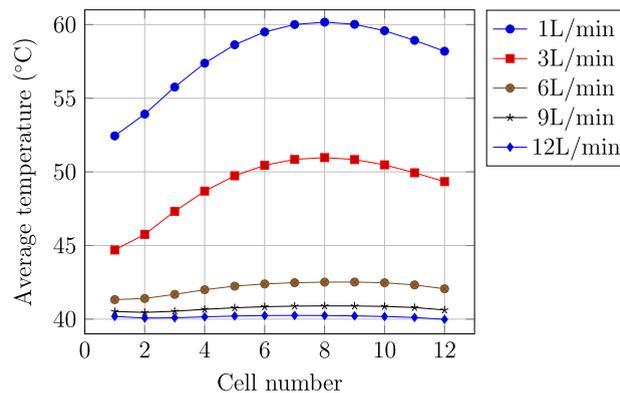


Fig. 4. Average cell temperatures under various coolant flow rates.

Table 8  
Temperature data from Fig. 3.

	No insert [°C]	Plastic [°C]	Aluminium [°C]	Copper [°C]
Cell 1	35.9	35.3	35.2	35.0
Cell 2	36.2	35.5	35.4	35.2
Cell 3	36.6	36.0	35.7	35.6
Cell 4	37.0	36.5	36.1	36.0
Cell 5	37.4	36.8	36.4	36.3
Cell 6	37.6	37.0	36.6	36.5
Cell 7	37.8	37.1	36.8	36.6
Cell 8	37.8	37.2	36.8	36.7
Cell 9	37.8	37.2	36.8	36.6
Cell 10	37.7	37.0	36.7	36.6
Cell 11	37.4	36.8	36.5	36.4
Cell 12	37.2	36.2	36.3	36.1

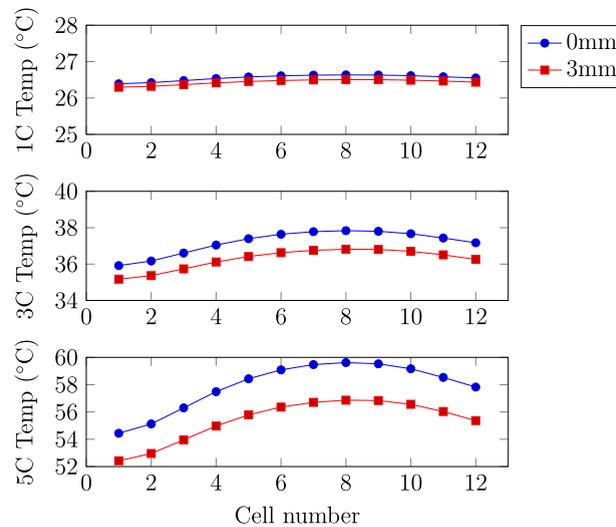
### 3.3. Effect of flow rate on module temperatures

The thermal performance of a battery module was analyzed for various coolant flow rates from 1 to 12 L/min. Material properties of aluminium was used for the 3 mm cooling insert. Steady state calculations were performed under 4C discharge rate. The coolant pressure drop and the temperature change between the cooling jacket inlet and outlet for all tested flow rates were also assessed.

As expected, results show higher pressure drops and lower temperatures with increasing flow rate due to higher convective heat transfer coefficient. The pressure drop increases monotonically with flow rate from around 62 Pa at 1 L/min to 2570 Pa at 12 L/min. Conversely, the coolant temperature difference between the outlet and the inlet decreases monotonically with increasing flow rate. At the slowest (1 L/min) and fastest (12 L/min) flow rates, the coolant temperature increased by around 10.7 °C and 0.8 °C, respectively. As shown in Fig. 4, flow rates above 8 L/min yielded very small improvements in temperature (less than 1 °C difference) with little to no difference in cooling performance. Significant average cell temperature reduction was observed between

**Table 9**  
Temperature data from Fig. 4.

	1 lpm [°C]	3 lpm [°C]	6 lpm [°C]	9 lpm [°C]	12 lpm [°C]
Cell 1	52.4	44.7	41.3	40.5	40.2
Cell 2	55.8	47.3	41.4	40.5	40.0
Cell 3	53.9	45.8	41.7	40.5	40.1
Cell 4	57.4	48.7	42.0	40.6	40.1
Cell 5	58.6	49.7	42.2	40.7	40.2
Cell 6	59.5	50.4	42.4	40.8	40.2
Cell 7	60.0	50.8	42.5	40.9	40.3
Cell 8	60.2	51.0	42.5	40.9	40.2
Cell 9	60.0	50.8	42.5	40.9	40.2
Cell 10	59.6	50.5	42.5	40.8	40.2
Cell 11	58.9	50.0	42.3	40.8	40.1
Cell 12	58.2	49.3	42.0	40.6	40.0



**Fig. 5.** Average cell temperatures with and without cooling insert under various C-rates.

1 and 6 L/min, from 60.2 °C to 42.5 °C in cell 8. However between 7 L/min and 12 L/min, average cell temperatures were only reduced from 41.7 °C to 40.2 °C in the same cell. Temperature uniformity follows a similar trend where between 1 and 6 L/min, the difference between the hottest and coldest cell was reduced from 7.7 °C to 1.2 °C. Between 7 L/min and 12 L/min, it was reduced from 0.81 °C to 0.27 °C. While higher flow rates reduce average cell temperatures and improve temperature uniformity of the module, its effectiveness quickly diminishes beyond 7 L/min. An optimal coolant flow rate must provide a good balance of pressure drop and cooling performance. For the given condition of 4C discharge rate and 3 mm thick aluminium cooling insert, 7 L/min coolant flow rate was determined to be the most effective overall (see Table 9).

### 3.4. Effect of C-rates on module temperature

The thermal performance of a battery module was evaluated for discharge rates from 1C to 5C. C-rates affect the heat generation in each battery cell as shown in Fig. 5. Numerical analyses were conducted at steady state, coolant flow rate of 4 L/min, and aluminium cooling insert thicknesses were varied from 0 to 3 mm. For all discharge rates, the average temperature reduction improved with higher cooling insert thickness. The effect was less pronounced at 1C to 2C (less than 0.5 °C), but the differences can exceed 2.5 °C at 5C and 3 mm thick cooling insert. Furthermore, temperature uniformity also decreased with higher discharge rates. Temperature uniformity worsened from 0.24 °C at 1C to 5.2 °C at 5C for modules without a cooling insert. Modules with a 3 mm thick cooling insert performed a bit better, from 0.21 °C at 1C to 4.4 °C at 5C. Significant temperature variations within a battery cell can accelerate capacity fade [60] and must be avoided. However, such temperature variations are unavoidable under the proposed design since cooling only occurs at the bottom of the battery cell.

Overall, the cooling insert design can lower average cell temperatures as well as temperature distribution within the module. It can also maintain cell temperatures to within 40 °C under steady discharge rate of 4C at all tested conditions. While safe temperature limit was exceeded at a steady 5C, high discharge rates in excess of 4C occurs infrequently and temporarily such that even a 3 mm thick cooling plate would be adequate (see Table 10).

**Table 10**  
Temperature data from Fig. 5.

	0 mm, 1C [°C]	0 mm, 3C [°C]	0 mm, 5C [°C]	3 mm, 1C [°C]	3 mm, 3C [°C]	3 mm, 5C [°C]
Cell 1	26.4	35.9	54.4	27.0	35.2	52.4
Cell 2	26.4	36.2	55.1	26.3	35.4	53.0
Cell 3	26.5	36.6	56.3	26.4	35.7	53.9
Cell 4	26.5	37.0	57.4	26.4	36.1	55.0
Cell 5	26.6	37.4	58.4	26.5	36.4	55.8
Cell 6	26.6	37.6	59.0	26.5	36.6	56.4
Cell 7	26.6	37.8	59.5	26.5	36.8	56.7
Cell 8	26.6	37.8	59.6	26.5	36.8	56.9
Cell 9	26.6	37.8	59.5	26.5	36.8	56.8
Cell 10	26.6	37.7	59.2	26.5	36.7	56.6
Cell 11	26.6	37.4	58.5	26.5	36.5	56.0
Cell 12	26.6	37.2	57.8	26.4	36.2	55.4

#### 4. Conclusions

Numerical thermofluidic analyses of a prismatic NCM Li-ion battery module integrated with a cooling insert were performed in this study. Thermal performances of the battery module were evaluated under various conditions such as cooling insert thickness and material, coolant flow rate, and discharge rate. The following conclusions can be drawn from the results.

1. A 3 mm thick cooling insert increased the heat flux into the TIM by up to 15.6% compared to a module without a cooling insert thereby enhancing cooling performance.
2. Various cooling insert materials were analyzed including plastic and two metals (copper and aluminium). Results showed 0.7 and 1.0 °C reduction in temperature for plastic and metallic inserts, respectively, indicating that the presence of a cooling insert can be a significant factor in lowering the module temperatures and improving its temperature uniformity.
3. Higher coolant flow rate significantly improved the cooling performance of the module up to a certain limit. For a discharge rate of 4C, the optimal flow rate was 7 L/min.
4. Higher discharge rate significantly increased the temperature differences within a cell but a 3 mm cooling insert was able to reduce this difference by up to 4 °C thereby improving the performance and durability of the battery module.
5. The results of this study could potentially lead to the development of a compact and low-cost intra-cell heat spreader in a battery module that can be readily implemented in production EVs.

#### CRedit authorship contribution statement

**Jeongwan Han:** Methodology, Data curation, Software, Roles/Writing – original draft. **Wonjin Ko:** Conceptualization, Investigation, Data curation. **Myung-Seop Lim:** Validation, Project administration. **Tonghun Lee:** Writing – review & editing, Resources. **Jihyung Yoo:** Funding acquisition, Writing – review & editing, Supervision.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

Data will be made available on request.

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