

# Analysis Strategy Considering Magnetic Saturation of Interior Permanent Magnet Synchronous Motors

<sup>1</sup>Young-Kyoun Kim, <sup>2</sup>Jung-Pyo Hong

<sup>1</sup>Artificial Intelligence & Mechatronics Research Center, <sup>2</sup>Mechanical engineering, Hanyang University

<sup>1</sup>Korea Electronics Technology Institute (KETI), Puchon 420-140, Korea

<sup>2</sup>#17, Hengang-dong, Seoul, 133-791, South Korea

ensigma@hitel.net, hongjp@hanyang.ac.kr

**Abstract** — This paper presents a method to calculate the motor performance of interior permanent magnet synchronous motors. Traditionally, the motor analysis is accomplished by using equivalent circuit, which consists of motor parameters including constant inductances. However, inductances are affected critically magnetic saturation according to both the load current and the current angle. This paper proposes the analysis method with considering fluctuations of these inductances.

## I. INTRODUCTION

Interior permanent magnet synchronous motors (IPMSM) are widely used in industrial applications, which require high power density. In the applications such as electric vehicles and compressor drives, the efficiency is one of the most important performances. The operating efficiency depends on the control strategies. Several control methods have been proposed in order to reduce the loss of IPMSM and improve their performance. One of the control strategies is the maximum torque-per-ampere current control. The possibility of operating methods depends on parameters of IPMSM. Therefore, the effects of magnetic saturation due to both the armature current and the current angle are dominant. Specially, the d- and q-axis inductances vary depending on the d- and q-axis current respectively, and as a result the control performances are affected by the magnetic saturation. This paper presents a simulation method to decide correct the current vector of IPMSM.

## II. SIMULATION OF IPMSM

An equivalent circuit analysis for IPMSM are based on a rotate synchronous d-q reference frame, and frequently used to simulate their performances. The mathematical model of the equivalent circuit is given as follow the voltage equations [1]-[2].

$$\begin{bmatrix} v_d \\ v_q \end{bmatrix} = \begin{bmatrix} R_s + pL_d & -\omega L_q \\ \omega L_d & R_s + pL_q \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \begin{bmatrix} 0 \\ \omega \Psi_a \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} \quad (1)$$

$$T = P_n \left\{ \Psi_a I_a \cos \beta + \frac{1}{2} (L_q - L_d) I_a^2 \sin 2\beta \right\} \quad (2)$$

Where  $i_d$  and  $i_q$  are d- and q-axis components of armature current,  $v_d$  and  $v_q$  are d- and q-axis components of terminal voltage,  $L_d$  and  $L_q$  are d- and q-axis components of armature self-inductances,  $R_s$  is armature resistance per phase,  $\Psi_a$  is  $\sqrt{3/2} \Psi_f$ ,  $\Psi_f$  is maximum flux-linkage due to

permanent magnet per phase,  $p$  is differential operator,  $P_n$  is number of pole pairs.  $\beta$  is current angle.

IPMSM has a saliency and the reluctance torque is available, the current vector is controlled in order to produce the maximum torque per current in the constant torque region. The condition of the maximum torque-per-ampere current control can be derived by differentiating equation (2) with respect to  $\beta$  and equating the derivatives to zero. As a result, the condition is given by [1]-[2]

$$\beta = \sin^{-1} \left\{ \frac{-\Psi_a + \sqrt{\Psi_a^2 + 8(L_q - L_d)^2 I_a^2}}{4(L_q - L_d) I_a} \right\} \quad (3)$$

The above equation is derived as if the magnetic saturation is ignored and  $L_d$  and  $L_q$  are assumed to be constant parameter. It seems that the operating performances become worse and the control system may become unstable.

Therefore, in order to improve the operating performances, the decision method of the current vector should be considering the effects of magnetic saturation. In this paper, the proposed computation method is based on the iteration algorithm shown in Fig. 1. Also, the iteration method can be solved by using a numerical optimization algorithm. In the proposed Method,  $L_d$  and  $L_q$  are calculated by FEA according to the d- and q-axis current [3] and used in the torque calculation. Fig. 2 and Fig 3 show the  $L_d$  and  $L_q$  of the prototype IPMSM. The  $L_d$  and  $L_q$  vary depending on the d- and q-axis current respectively.

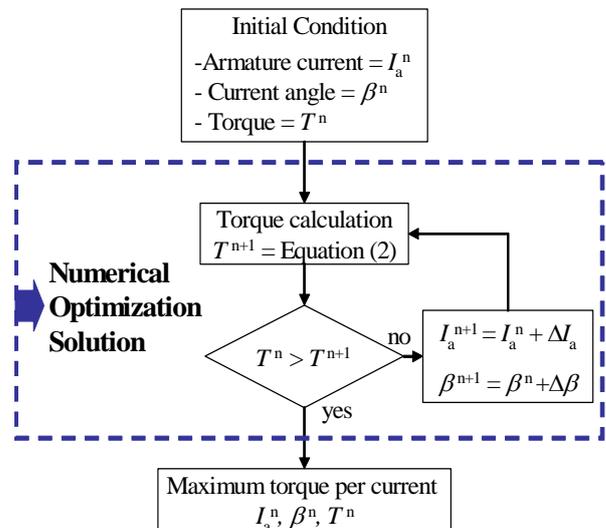


Fig. 1. Flow-chart of the proposed simulation method

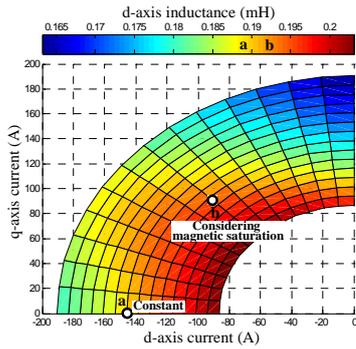


Fig. 2.  $L_d$  profile according to the d- and q-axis current

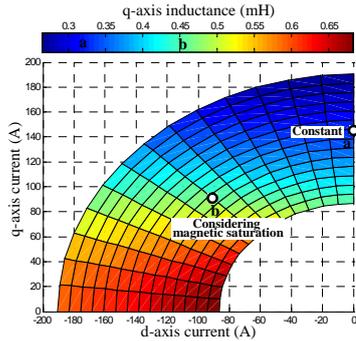


Fig. 3.  $L_q$  profile according to the d- and q-axis current

### III. SIMULATION RESULTS

The parameters of the prototype IPMSM are listed in Table I, When d-axis is placed in the direction of resistance as shown in Fig. 4.a,  $L_d$  is a value at  $i_d=145A$ ,  $i_q=0A$ , and when q-axis is placed in the direction of least resistance as shown in Fig. 4.b,  $L_q$  is a value at  $i_q =145A$ ,  $i_d=0A$ . The simulation results of the torque and the terminal voltage controlled by the maximum torque-per-current control are shown in Fig. 5. The solid-circle curves represent the calculated characteristics without consideration of the magnetic saturation, in which the constant value of inductances (listed Table 1.) and equation (3) are used. The open-circle curves represent the calculated characteristics with consideration of magnetic saturation, in which the value of inductances is based on both Fig 2 and Fig3 according to the d- and q-axis current. Fig. 5. shows the calculated results of the armature current and current angle, and Fig. 6. shows the computed results of the power and efficiency.

TABLE I  
SPECIFICATION OF PROTOTYPE IPMSM

Parameters	Value	Unit
Number of Phase	3	phase
Number of Pole	4	pole
DC linkage Voltage	42	V
Rated Speed	3500	rpm
Rated Torque	9.8	N-m
Back-emf coefficient	3.49	mV/rpm
Resistance per a phase	12.5	mΩ
$L_d$	0.188	mH
$L_q$	0.324	mH
Maximum current	145	A

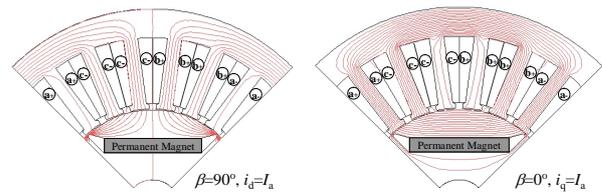


Fig. 4. Cross section of IPMSM

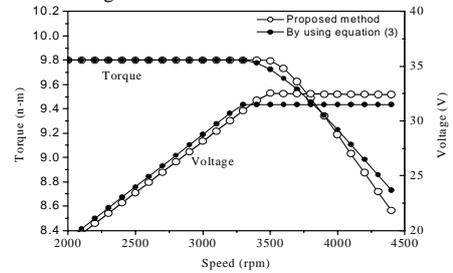


Fig. 5. Torque and voltage characteristics of prototype IPMSM

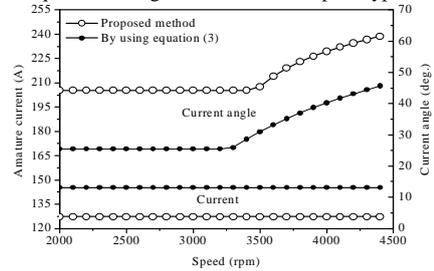


Fig. 6. Armature current and angle characteristics of prototype IPMSM

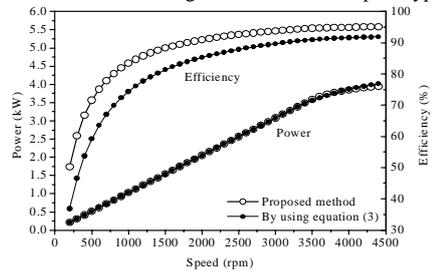


Fig. 7. Efficiency and power characteristics of prototype IPMSM

### IV. CONCLUSION

The consideration of magnetic saturation was proposed for the analysis method of the IPMSM performance in this paper. The  $L_d$  and  $L_q$  of IPMSM vary depending on the d- and q-axis current because of the magnetic saturation. The  $L_d$  and  $L_q$  are simply used as the proposed analysis method. It can be considered that the ability of the proposed method is useful for the analysis of operating performances of the IPMSM.

### V. REFERENCES

- [1] Murakami, H., Honda, Y., Kiriya, H., Morimoto, S., Takeda, Y., F. Henrotte and K. Hameyer, "The performance comparison of SPMSM, IPMSM and SynRM in use as air-conditioning compressor ", Ind. Appl. Conference, 32(1):840-845, Oct. 1999.
- [2] T. Sebastian, G.R. Slemon, and M.A. Rahman, "Modelling of Permanent Magnet Synchronous Motors," *IEEE Trans. on Magn.*, vol. 22, No. 5, pp. 1069-1071, Sept. 1986.
- [3] Sheppard J. Salon, *Finite Element Analysis of Electrical Machines*, Kluwer Academic Publishers.



**Proceedings  
of the**

**16<sup>th</sup> Conference on the Computation of  
Electromagnetic Fields**

# **COMPUMAG 2007**

**June 24<sup>th</sup> - 28<sup>th</sup>**

**Aachen, Germany**

## Wednesday, June 27<sup>th</sup>

### OC1 – Optimisation - Software Methodology

EUROPA SAAL

08:30–10:10 Session chair: **Gabriela Ciuprina, Jan Sykulski**

- |               |   |     |
|---------------|---|-----|
| <b>IPC-1</b>  | <i>Parallel Computers Everywhere</i><br>Prof. Dr. Christian Bischof, GERMANY  | 693 |
| <b>*OC1-1</b> | <i>A New Strategy for Reducing Communication Latency in Parallel 3-D Finite Element Tetrahedral Mesh Refinement</i><br>Da Qi Ren, Steve Mcfee, Dennis Giannacopoulos, CANADA                                  | 701 |
| <b>*OC1-2</b> | <i>Analysis of the Computational Cost of Approximation-based Hybrid Evolutionary Algorithms in Electromagnetic Design</i><br>Frederico Gadelha Guimaraes, David Alister Lowther, Jaime Arturo Ramirez, BRAZIL | 703 |
| <b>OC1-3</b>  | <i>Dynamic Multiobjective Optimization: a Way to the Shape Design with Transient Fields</i><br>Paolo Di Barba, ITALY  | 705 |

### PC1 – Electrical Machines and Drives

BALUSTRAD

10:30–12:10 Session chair: **Erich Schmidt, Yoshihiro Kawase**

- |              |   |     |
|--------------|---|-----|
| <b>PC1-1</b> | <i>An Improved Design for Steady-Static Characteristic of Permanent Magnet Type Step Motor with Claw Poles by 3D FEM</i><br>Dae-Sung Jung, Seung-Bin Lim, Ju Lee, SOUTH KOREA | 707 |
| <b>PC1-2</b> | <i>Holding Torque Characteristics Analysis of Permanent magnet Spherical Motor</i><br>Sung Hong Won, Tae Heoung Kim and Ju Lee, SOUTH KOREA                                   | 709 |
| <b>PC1-3</b> | <i>Characteristic Analysis of Claw-pole Generator using Equivalent Magnetic Circuits</i><br>Sang-Ho Lee, Soon-O Kwon, Jung-Pyo Hong, Yang-Soo Lim, Yoon Hur, SOUTH KOREA      | 711 |
| <b>PC1-4</b> | <i>Design and Analysis of Switched Reluctance Motor Working at Optimum Operating Point</i><br>Jian Li, In-Jae Lee, Yunhyun Cho, SOUTH KOREA                                   | 713 |

<b>PC1-5</b>	<i>Analysis of PWM Vector Controlled Squirrel Cage Induction Motor during Eccentricity Rotor Motion Using FEM</i> Mi Jung Kim, Byung-Kuk Kim, Ji-Woo Moon, Yun-Hyun Cho, Don-Ha Hwang, Dong-Sik Kang, SOUTH KOREA	715
<b>PC1-6</b>	<i>Influence of Load Fluctuations upon Diagnosis of Mixed Eccentricity Fault In Induction Motors using Time Stepping Finite Element Method</i> Jawad Faiz, B.M. Ebrahimi, IRAN	717
<b>PC1-7</b>	<i>Synthetic Flux Linkage Identification for Interior Buried Permanent Magnet Synchronous Motor considering Cross-Magnetization</i> Sang-Yong Jung, Cheol-Gyun Lee, Sung-Chin Hahn, Sang-Yeop Kwak, Hyun-Kyo Jung, SOUTH KOREA	719
<b>PC1-8</b>	<i>Determination of Parameters Considering Magnetic Nonlinearity in Solid Core Transverse Flux Linear Motors for Dynamic Simulation</i> Ji-Young Lee, Ji-Won Kim, Jung-Hwan Chang, Do-Hyun Kang, and Jung-Pyo Hong, SOUTH KOREA	721
<b>PC1-9</b>	<i>Analysis Strategy Considering Magnetic Saturation of Interior Permanent Magnet Synchronous Motors</i> Young-Kyoun Kim, Jung-Pyo Hong, SOUTH KOREA	723
<b>PC1-10</b>	<i>Performance Computation of Claw-Pole Type Alternator based 3 Dimension Finite Element Method and Fourier Series</i> Seung-Bin Lim, Ki-Chan Kim, Go Sung Chul, Sang-Hwan Ham, SOUTH KOREA	725
<b>PC1-11</b>	<i>Flux-Weakening Performance and Output Power Capability of Permanent Magnet Synchronous Motors with Different Permanent Magnet Arrangement</i> Bojan Stumberger, Gorazd Stumberger, Miralem Hadziselimovic, Marko Jesenik, Anton Hamler, Mladen Trlep, SLOVENIA	727
<b>PC1-12</b>	<i>Arc models for simulation of brush motor commutations</i> Jerome Cros, Geraldo Sincero, Philippe Viarouge, CANADA	729
<b>PC1-13</b>	<i>Torque Ripple Reduction of Interior Permanent Magnet Synchronous Motor Using Harmonic Injected Current</i> Ji-Hyung Bahn, Sung-Il Kim, Geun-Ho Lee, Jung-Pyo Hong, SOUTH KOREA	731
<b>PC1-14</b>	<i>Investigation of Parameters Variation and Radial Magnetic Forces by Pole-Slot Combinations in Interior Permanent Magnet Synchronous Motor with Concentrated Winding</i> Seung-Hyoung Ha, Sang-Ho Lee, Soon-O Kwon, Jung-Pyo Hong, SOUTH KOREA	733

<b>PC1-15</b>	<i>Accurate induction motor estimator based on magnetic field analysis</i> Dimitrios S. Raptis, Antonios G. Kladas and John A. Tegopoulos, GREECE	735
<b>PC1-16</b>	<i>Power Generation Optimization from Sea Waves by using a Permanent Magnet Linear Generator Drive</i> N. M. Kimoulakis, A. G. Kladas and J. A. Tegopoulos, GREECE	737
<b>PC1-17</b>	<i>Study on the Characteristics for A Novel Segmental Switched Reluctance Motor</i> Tao Sun, Ji-Young Lee, Jung-Pyo Hong, SOUTH KOREA	739
<b>PC1-18</b>	<i>Determination of Parameters of Motor Simulation Module Employed in ADVISOR</i> Tao Sun, Suk-Hee Lee, Soon-O Kwon Jung-Pyo Hong, SOUTH KOREA	741
<b>PC1-19</b>	<i>Analysis of Transient Short Circuit Electromagnetic Forces in Isolated Phase Buses</i> Arash Hassanpour Isfahani, Sadegh Vaez-Zadeh, IRAN	743
<b>PC1-20</b>	<i>Coupling Boundary Element and Permeances Network Methods for Modeling Permanent Magnet Motors in automotive applications</i> Said Touati, J. A. Farooq, A. Djerdir, R. Ibtouen, A. Miraoui, O. Touhami, ALGERIA	745
<b>PC1-21</b>	<i>Optimum Design for Eddy Current Reduction in IPMSM</i> Jaewoo Jung, Soon-O Kwon, Ji-Hyung Ban, Jung Pyo Hong, SOUTH KOREA	747
<b>PC1-22</b>	<i>Design of a Permanent Magnet Assisted Synchronous Reluctance Motor for Integrated Starter and Generator in 42 Volt System of Vehicles</i> Yang-Su Lim, Dong-Hun Lee, Yoon Hur, Jae-Woo Jung, Jung-Pyo Hong, SOUTH KOREA	749

PC2 – Numerical Techniques

BALUSTRADÉ

10:30–12:10 Session chair: **Igor Tsukerman, Georg Wimmer**

<b>PC2-1</b>	<i>An Adaptive Remeshing Technique Insuring High Quality Meshes</i> Marcel Ebene-Ebene, Y. Marechal, D. Armand, D. Ladas, FRANCE	751
--------------	---	-----