

# The comparison of characteristic and operating performance by pole-slot combinations in Interior Permanent Magnet Synchronous Motor with concentrated winding

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**Abstract--** The Interior Permanent Magnet Synchronous Motor (IPMSM) is widely used for several industrial applications, because the motor can have high performance due to the reluctance torque generated by the difference of d-q axes inductance, and then the motor has much more torque than the Surface Permanent Magnet Synchronous Motor (SPMSM).

In order to miniature and improve the manufacture efficiency of the motor, it has concentrated winding, because concentrated winding can reduce the motor volume and make the manufacture be simpler compared with the distributed winding. When motor with concentrated winding is designed, pole-slot combinations are very important. In accordance with pole-slot combinations, the winding factor can be increased, and at the same time d-q axes inductance and saliency ratio are influenced. The parameters, such as back electromotive force (BEMF), d-q axes inductance, and saliency ratio, are very important which influent characteristics of the motor and operating performance. Therefore, this paper presents the comparison of characteristics and operating performance by pole-slot combinations in IPMSM with concentrated winding.

**Index Terms**—concentrated winding, interior permanent magnet synchronous motor, pole-slot combinations, winding factor.

## I. INTRODUCTION

Permanent magnet motors (PM motors) have a wide application because they offer excellent maintainability, controllability, and environmental endurance while providing high-efficiency operation at high power factor [1].

Interior Permanent Magnet Synchronous Motor (IPMSM) has high energy density, compared with Surface Permanent Magnet Synchronous Motor (SPMSM) because it has reluctance torque by difference of d-q axes inductance in addition to magnetic torque by the permanent magnet, and be easy using flux weakening control at constant power operation. Therefore IPMSM is increasingly employed for electric vehicles and compressor drives.

The winding layouts of motor generally are divided into two layouts that are concentrated winding and distributed winding. The concentrated winding has shorter end winding and simpler structure suitable for high volume automated manufacturing in comparison with the distributed winding [2].

The motors with concentrated windings usually have low winding factors, and so have a low back electromotive force (BEMF). However winding factors can be increased in accordance with pole-slot combinations.

The winding factors also have influence upon d-q axes inductance. BEMF and d-q axes inductance which are important design parameters determine on constant torque region and constant power operation. Therefore winding factors in accordance with pole-slot combinations are very important factors.

The aim of this paper is to investigate design parameters and operating performance of IPMSM with different winding factors in accordance with pole-slot combinations.

## II. WINDING FACTOR

IPMSM with concentrated windings usually has slot number of only 2/3 pole numbers, which results in a poor fundamental winding factor of 0.866. This can be compared to the ideal winding factor of one, which can easily be acquired using distributed windings [2]. However, by choosing better pole-slot combinations, the winding factor can be substantially increased.

Table I shows the results of winding factors from 4 poles to 16 poles and from 6 slots to 24 slots.

TABLE I  
WINDING FACTOR

Pole Slot	4	6	8	10	12	14	16
6	0.866		0.866	0.500		0.500	0.866
9	0.617	0.866	0.945	0.945	0.866	0.617	0.328
12			0.866	0.933		0.933	0.866
15			0.711	0.866		0.951	0.951
18				0.735	0.866	0.901	0.945
21						0.866	0.891
24						0.760	0.866

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### III. THE COMPARISON OF DESIGN PARAMETERS

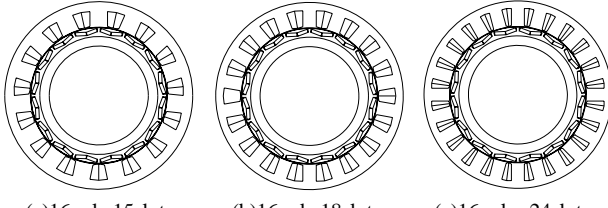


Fig. 1. Three motor models.

In order to compare parameters of motor with different winding factors, three motor models are chosen and analyzed. In this paper three models are selected as shown in Fig.1. Fig.1 (a), (b) and (c) are 16poles 15slots, 16poles 18slots and 16poles 24slots models which are defined as model1, model2 and model3. Their winding factors are 0.866, 0.945 and 0.951 respectively. Finite Element Method (FEM) is used to calculate some parameters such as line-line BEMF, Total Harmonic Distortion (THD), cogging torque, saliency ratio. Having the same rotor structure, PM volume and fill-factor, the ratios of tooth width and yoke width in the three models are 1.86, 1.67 and 1.73 respectively.

#### A. Back EMF, THD, Cogging Torque

The Fig. 2 and Table II show line-line BEMF of model1, 2 and 3. Among three models, line-line BEMF of model1 is the largest and the most sinusoidal. Therefore THD of model1 is the lowest.

Cogging torque of three models is compared as shown in Fig. 3 and Table II. It is obvious that model1 has the lowest cogging torque. The line-line BEMF and cogging torque peak-peak value of model1 are chosen as the standard. And then values of the other two models are normalized.

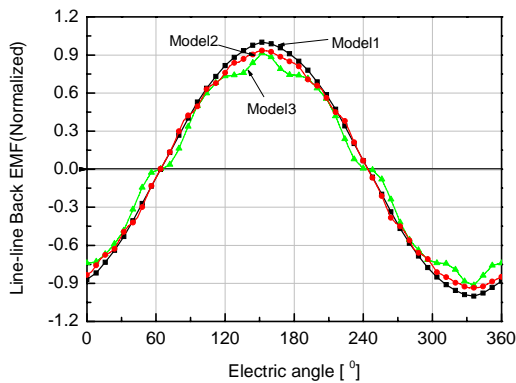
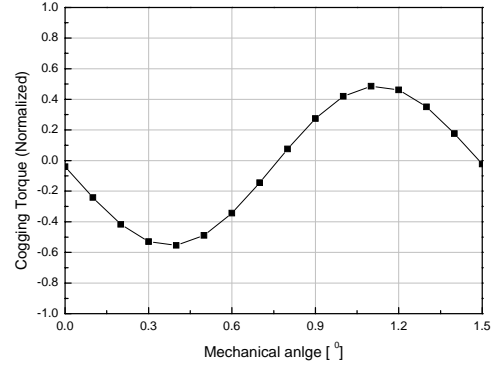


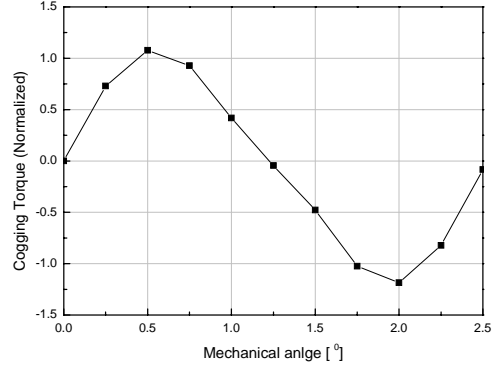
Fig. 2 The comparison of line-line Back EMF.

TABLE II  
LINE-LINE BACK EMF, THD, COGGING TORQUE

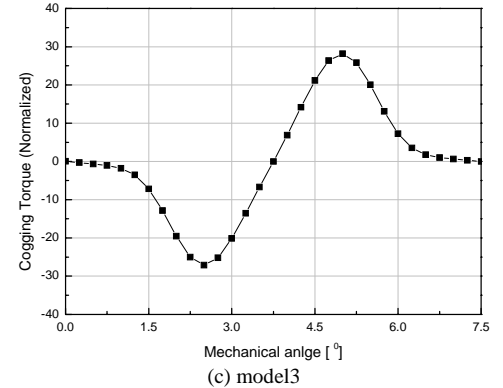
Model	Model1	Model2	Model3
Contents			
Line-Line Back EMF(Normalized)	1	0.944	0.865
Winding Factor	0.951	0.945	0.866
THD(%)	0.71	3.28	9.2
Cogging Torque peak-peak(Normalized)	1	2.27	55.27



(a) model1



(b) model2



(c) model3

Fig. 3 Cogging torque of three models.

#### B. Torque and Torque ripple

Torque of IPMSM in normal operation is expressed in d-q coordinates as shown in equation (1). Torque of IPMSM is composed of magnetic torque and reluctance torque.

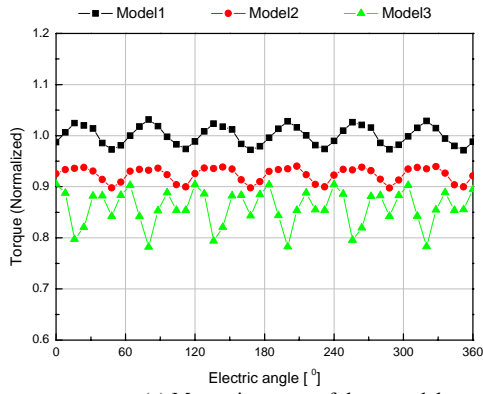
$$\begin{aligned}
 T &= P_n \{ \psi_a i_q + (L_d - L_q) i_d i_q \} \\
 &= P_n \{ \psi_a i_a \cos \beta + \frac{1}{2} (L_q - L_d) I_a^2 \sin 2\beta \}
 \end{aligned} \quad (1)$$

where  $P_n$  is pole pair number,  $\psi_a = \sqrt{3/2} \psi_f$ ,  $\psi_f$  is peak armature flux linkage due to permanent magnets,  $i_d, i_q$  are d-q components of armature current,  $L_d, L_q$  are inductance along d-q axes,  $I_a = \sqrt{3} I_e$ ,  $I_e$  is effective value of armature current,  $\beta$  is lead angle of current vector from q axis.

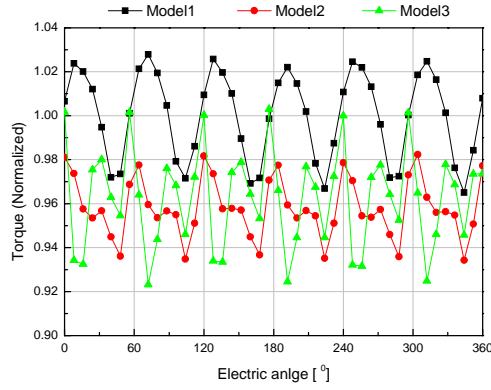
In order to compare torque and torque ripple of

model1, 2 and 3 with same current, the lead angle of current vector from q axis at the maximum torque must be checked. And the values of three models are  $16^\circ$ ,  $16^\circ$  and  $24^\circ$ . Also the torque is calculated at  $\beta = 0$  in order to confirm magnetic torque. The reluctance torque can be calculated by subtracting magnetic torque from maximum torque.

Fig. 4 and Table III show magnetic torque, reluctance torque,  $\beta$  at maximum torque, average torque and torque ripple. These parameters values of model1 are chosen as standard. And then values of the other two models are normalized. The results of average torque are same values but torque ripple and reluctance torque of model3 are largest. On the other hand, magnetic torque of model3 is lowest because Line-line BEMF of model3 is lowest.



(a) Magnetic torque of three models.



(b) Average torque of three models.

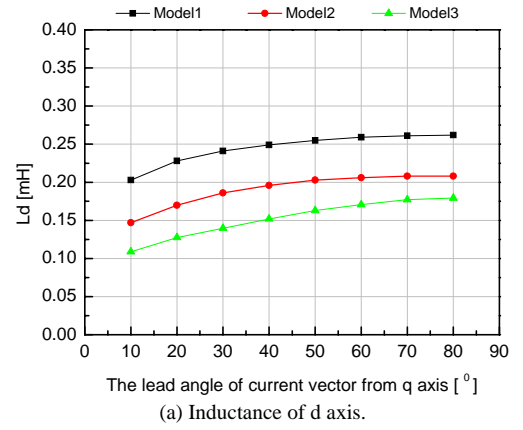
Fig. 4. Torque analysis.

TABLE III  
THE RESULTS OF TORQUE

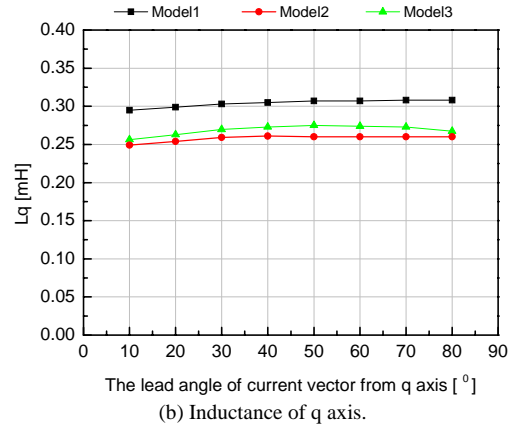
Contents \ Model	Model1	Model2	Model3
Magnetic Torque (Normalized)	1	0.924	0.860
Reluctance Torque (Normalized)	1	2.81	6.52
$\beta$ at the maximum torque ( $^\circ$ )	16	16	24
Average torque (Normalized)	1	0.958	0.963
Torque ripple (%)	6.3	5.02	8.3

### C. D-q axes inductance and Saliency ratio

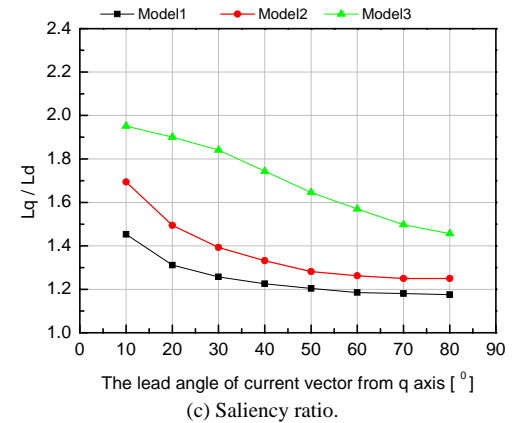
Since IPMSM has permanent magnet embedded in the rotor, it has a difference of d-q axes inductance. In case of saliency ratio which is defined as  $L_q/L_d$  is increased, reluctance torque will be increased. Fig. 5 (a), (b) and (c) show d-q axes inductance and saliency ratio of three models which are calculated from  $\beta = 10^\circ$  to  $\beta = 80^\circ$ . The d axis inductance increases in order of model3, model2 and model1, and then the q axis inductance increases in order of model2, model3 and model1. Saliency ratio of Model3 is the largest due to the lowest d axis inductance. Therefore reluctance torque of model1 is the lowest as shown in Table III.



(a) Inductance of d axis.



(b) Inductance of q axis.



(c) Saliency ratio.

Fig. 5. D-q axes inductance and saliency ratio.

#### IV. OPERATING PERFORMANCE

Voltage equation of IPMSM in normal operation is expressed in d-q coordinates as shown in equation (2).

$$\begin{bmatrix} v_d \\ v_q \end{bmatrix} = \begin{bmatrix} R_a + pL_d & -\omega L_q \\ \omega L_d & R_a + pL_q \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \begin{bmatrix} 0 \\ \omega \psi_a \end{bmatrix} \quad (2)$$

Where  $i_d, i_q$  are d-q components of armature current,  $v_d, v_q$  are d-q components of armature voltage,  $\psi_a = \sqrt{3/2} \psi_f$ ,  $\psi_f$  is peak armature flux linkage due to permanent magnets,  $R_a$  is armature resistance,  $L_d, L_q$  are inductance along d-q axes,  $p = d/dt$ .

Various methods of current vector control have been proposed using the above d-q model. Since IPMSM is fed via inverter, the following limitations on armature current and terminal voltage must be considered.

$$I_a = \sqrt{i_d^2 + i_q^2} \leq I_{am} \quad (3)$$

$$V_a = \sqrt{v_d^2 + v_q^2} \leq V_{am} \quad (4)$$

Where  $I_{am}$  and  $V_{am}$  are ceiling values of current and voltage [1].

When maximum power control is executed, constant power operation region is determined by machine parameters, and pattern of speed-power characteristic is known to depend on  $\psi_{d \min}$

$$\psi_{d \min} = \psi_a - L_d I_{am} \quad (5)$$

$\psi_{d \min}$  is the difference between flux linkage caused by permanent magnets, and maximum negative flux linkage caused by armature reaction along d-axis, which corresponds to minimum flux linkage along d-axis [3-4].

For  $\psi_{d \min} > 0$ , there is an output limit as follows.

$$\omega_c = \frac{V_{om}}{\psi_a - L_d I_{am}} = \frac{V_{om}}{\psi_{d \min}} \quad (6)$$

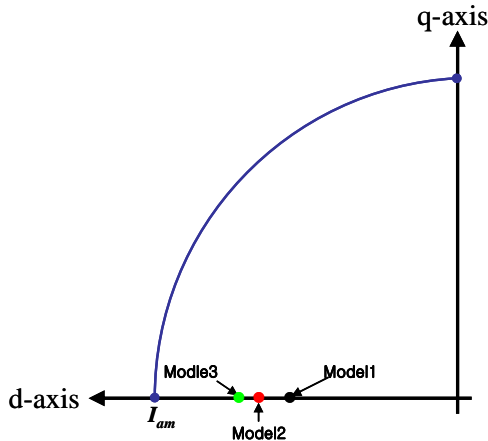


Fig. 6.  $\psi_a/L_d$  of the three models.

The more  $\psi_{d \min}$ , the larger the maximum torque is, but at the same time, constant power operation region becomes narrow. On the other hand,  $\psi_{d \min} \leq 0$ , there is no operating limit theoretically, and the less the absolute value of  $\psi_{d \min}$ , the larger is the output. Thus,  $\psi_{d \min} = 0$  is the ideal condition to obtain very wide range of constant power [1].

As equation (5),  $\psi_a/L_d$  value is  $I_{am}$  in the case of  $\psi_{d \min} = 0$ . The  $\psi_a/L_d$  values of the three models are lower than  $I_{am}$  as shown in the Fig. 6. Therefore, three models are no operating limit at high-speed region. The  $\psi_{d \min}$  value of model1 is the lowest because d axis inductance of Model1 is the lowest.

#### V. CONCLUSIONS

The results of design parameters of three models which have different winding factors show that design parameters, such as line-line BEMF, THD and cogging torque, of model3 are the best. However saliency ratio of model3 is the lowest.

The results of  $\psi_a/L_d$  values in the three models, which determines the constant torque region and the constant power region satisfy the power at the high-speed because the  $\psi_a/L_d$  value of these models is lower than  $I_{am}$ .

As mentioned above the results of design parameters and operating performance of model3 which has the largest winding factor are the best. Therefore choose of pole-slot combinations is important at initial design.

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## Welcome Message

Dear Colleagues,

It is a real pleasure and an honor for us to announce the 9th International Conference on Electrical Machines and Systems (ICEMS 2006) organized by the IEEJ Industry Applications Society (IAS).

ICEMS is the only major international conference devoted entirely to electrical machines and systems in Asia and provides an excellent opportunity for scientists and experts from all parts of the world to present recent developments and to exchange useful information and experiences from their research. In this conference, four outstanding professors are scheduled to offer presentations.

ICEMS 2006 concludes the first technical co-sponsorship with IEEE IAS. Each committee has been making every effort in the careful preparation of ICEMS 2006. We sincerely hope that ICEMS 2006 shall conclude successfully and ICEMS will go on to develop further as an important conference in this field.

On behalf of all the Committees of ICEMS 2006, I would like to say that we welcome you to the 9th International Conference on Electrical Machines and Systems (ICEMS 2006).

Sincerely,

Prof. Ichiro Miki  
ICEMS 2006 Conference Chairman  
October 23, 2006

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